



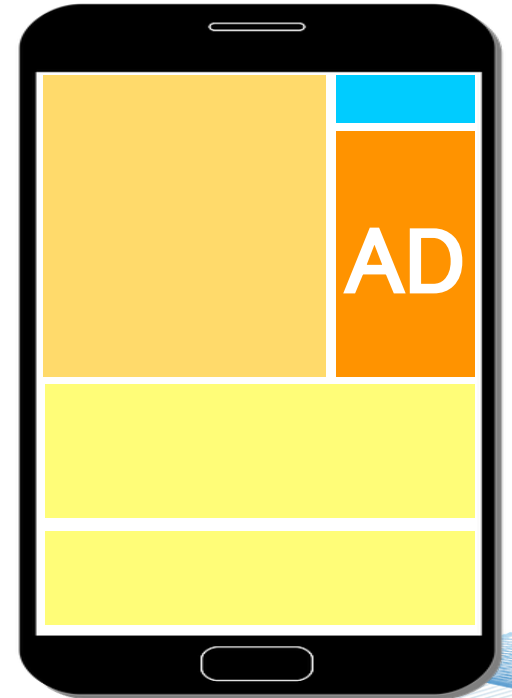
# Overview

- 1. Introduction**
- 2. Our approach**
- 3. Experiments**
- 4. Summary**

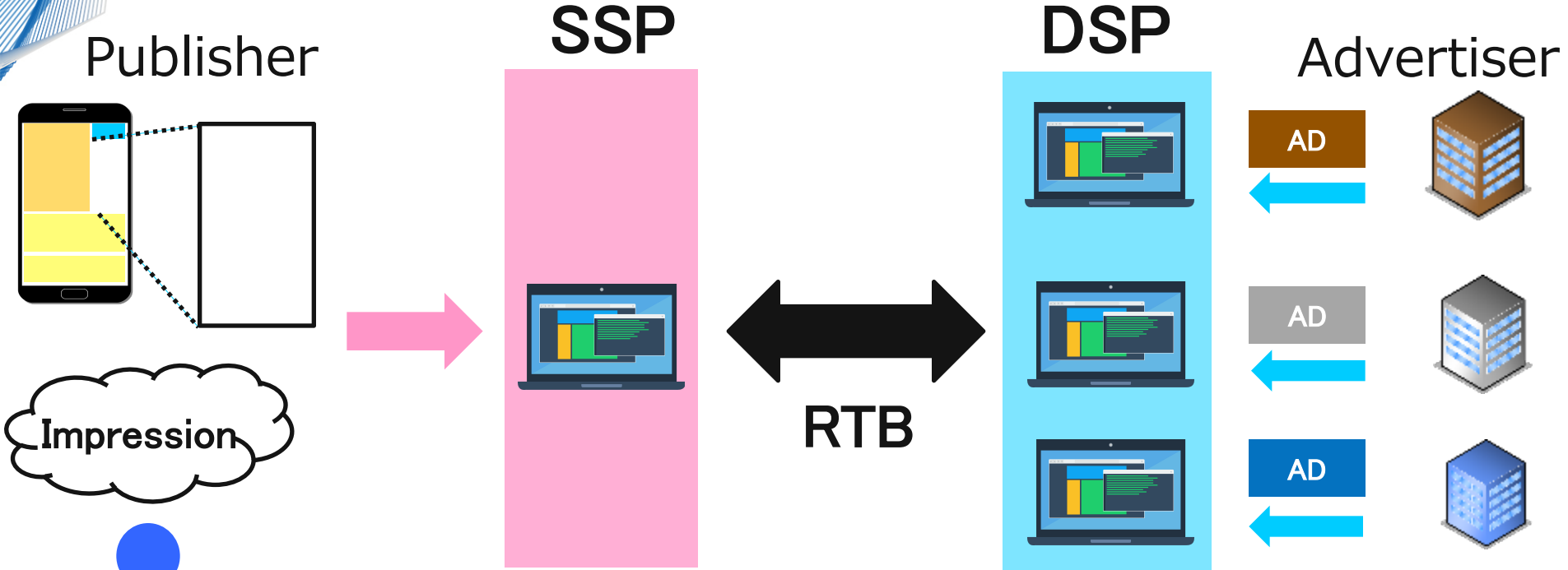
# 1. Introduction

- What is Display Advertising?
  - Advertisements appearing on **websites**
- Main purpose
  - Deliver general advertisements and brand messages

## Example of Display AD



# Behind the Scenes

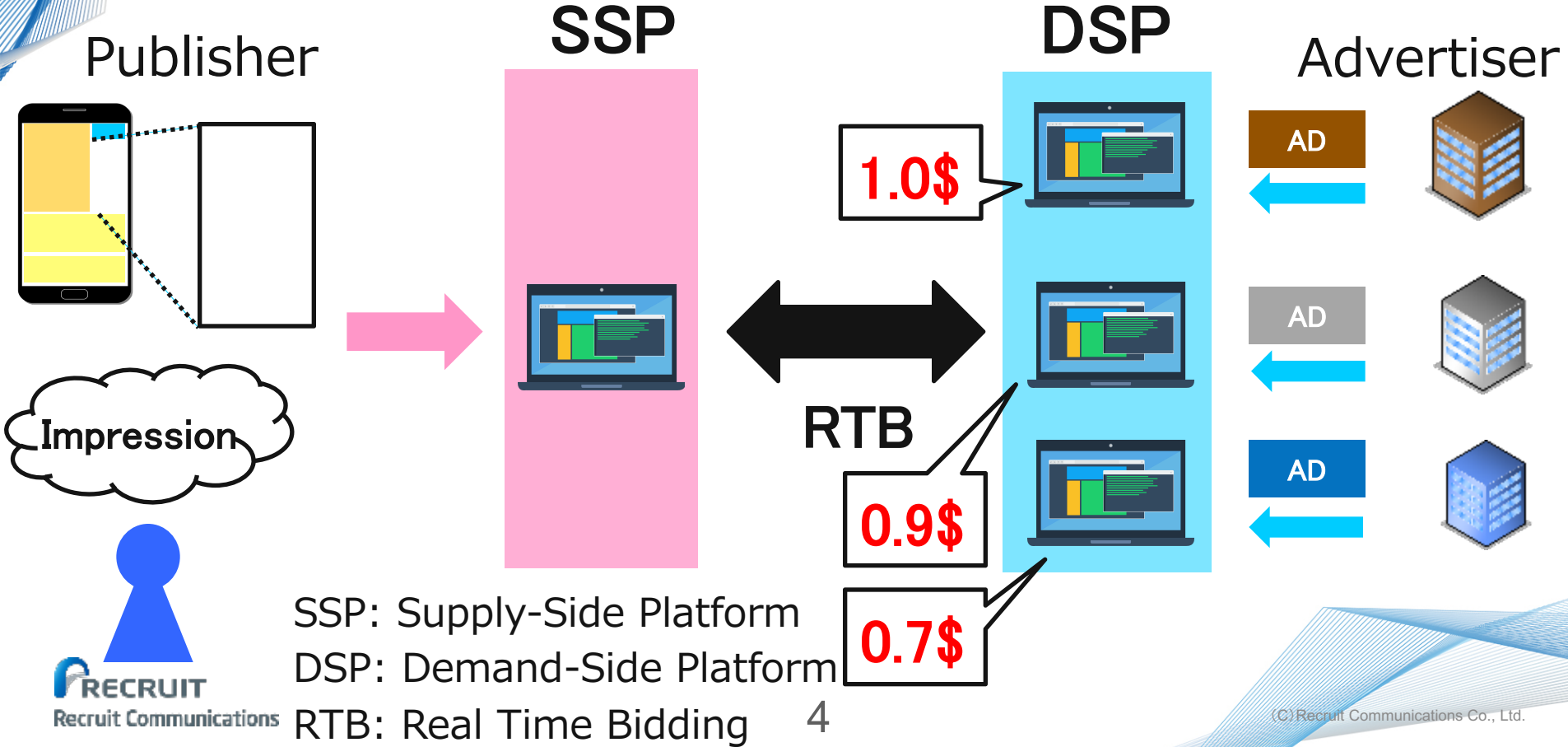


Impression

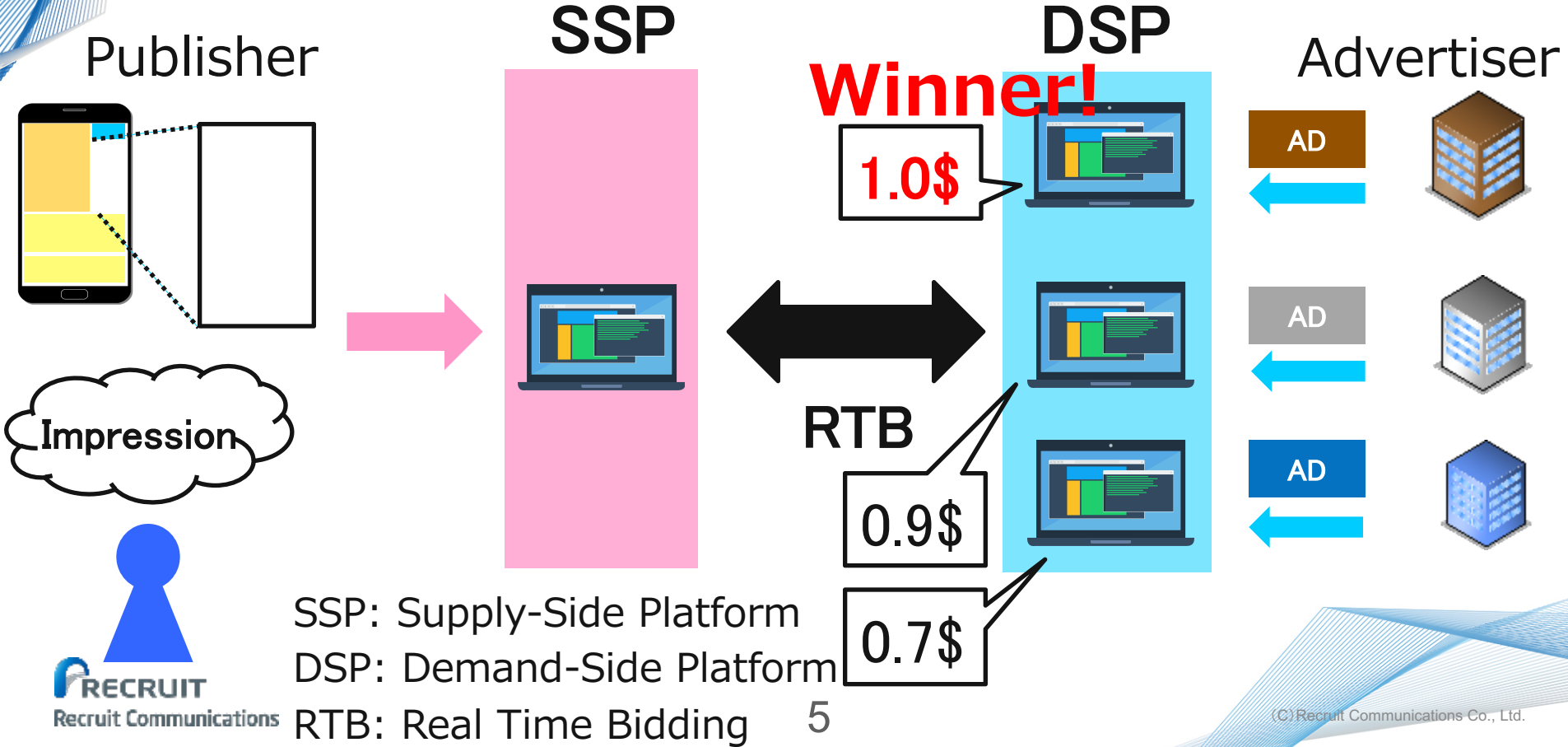


SSP: Supply-Side Platform  
DSP: Demand-Side Platform  
RTB: Real Time Bidding

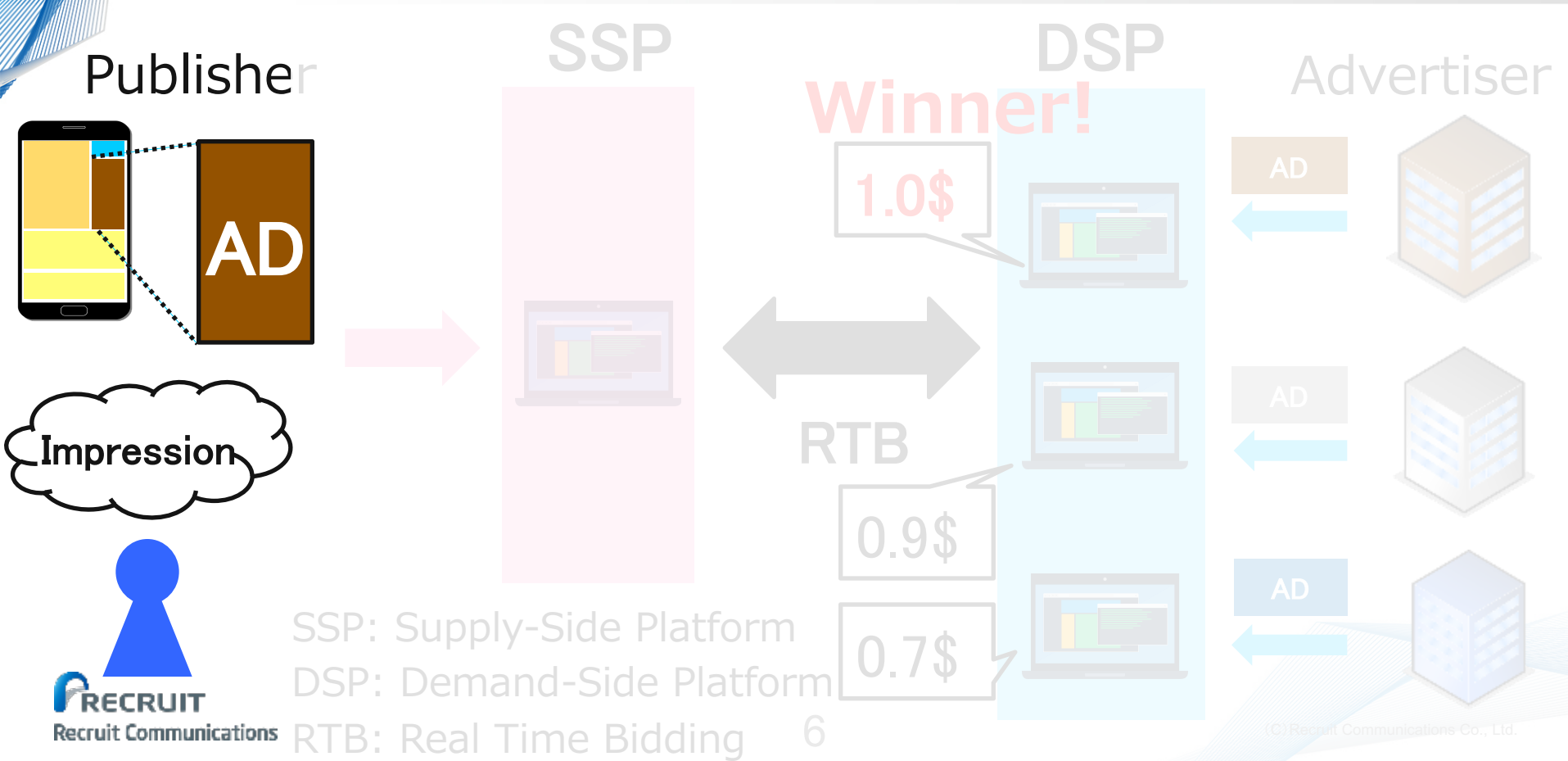
# Behind the Scenes



# Behind the Scenes



# Behind the Scenes



# Business Model

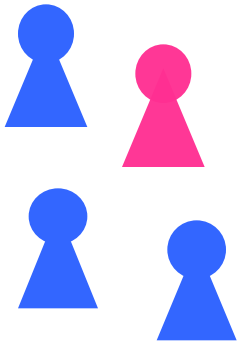
- Advertiser **pays** a publisher **when the ad is clicked**
- Performance Indicator
  - **Click Through Rate (CTR)**
  - Cost Per Impression (CPI)
  - Cost Per Click (CPC) ...etc

# CTR Prediction with Machine-Learning

(Click-through-rate)

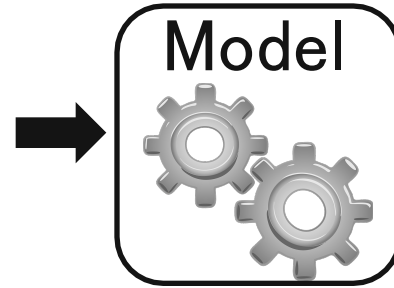
- Machine-Learning (ML) tech is often used for CTR prediction
- ML has succeeded in this field

Users

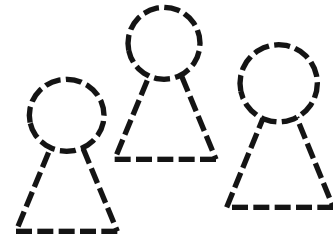


Matrix expression

Click	F1	F2	F3
1	M	01	2.13
0	F	07	2.12
0	F	23	4.2
?	F	99	1.2



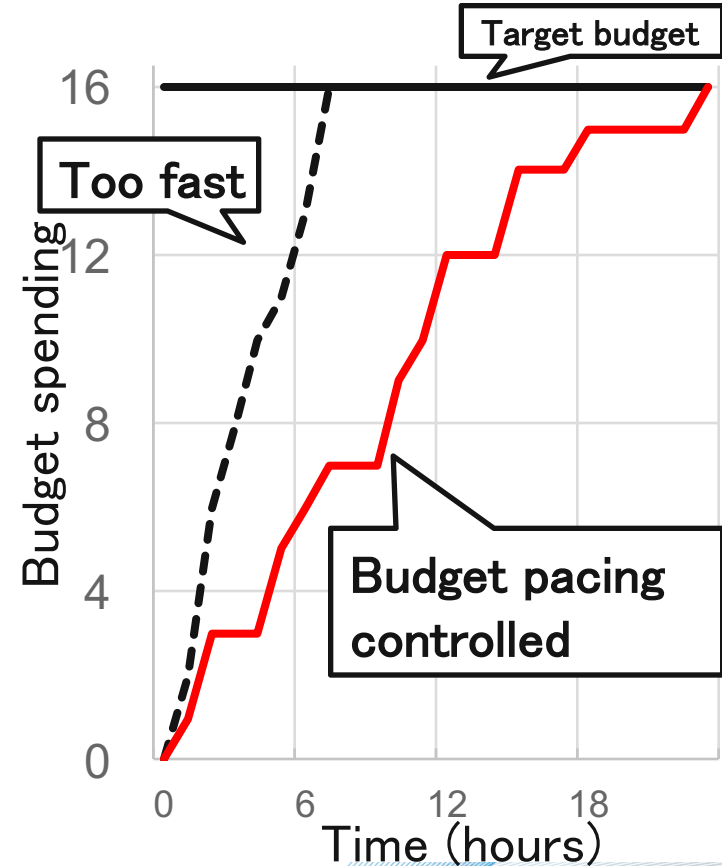
Click or Not Prediction





# Budget Pacing

- **Budget pacing** is also important
- Control of budget pacing helps advertisers to...
  - Reach a wider range of audience
  - Avoid a premature campaign stop / overspending



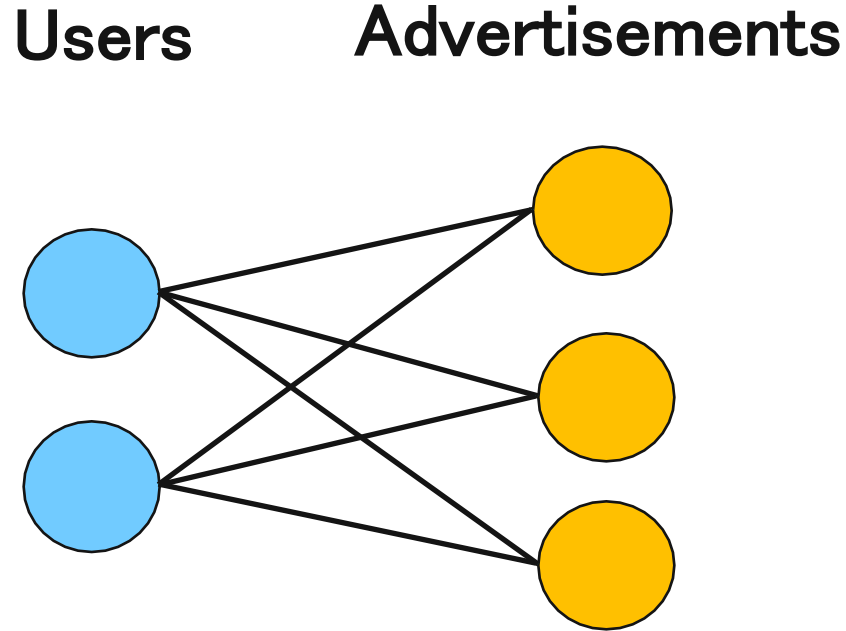
# Budget Pacing

- Two lines of strategies
  - Bid modification
  - Probabilistic throttling
- We propose a different way based on a bipartite graph and inspired by financial theory
- Our research strengthens existing research rather than replacing it

# Our Approach: Model and Formulation

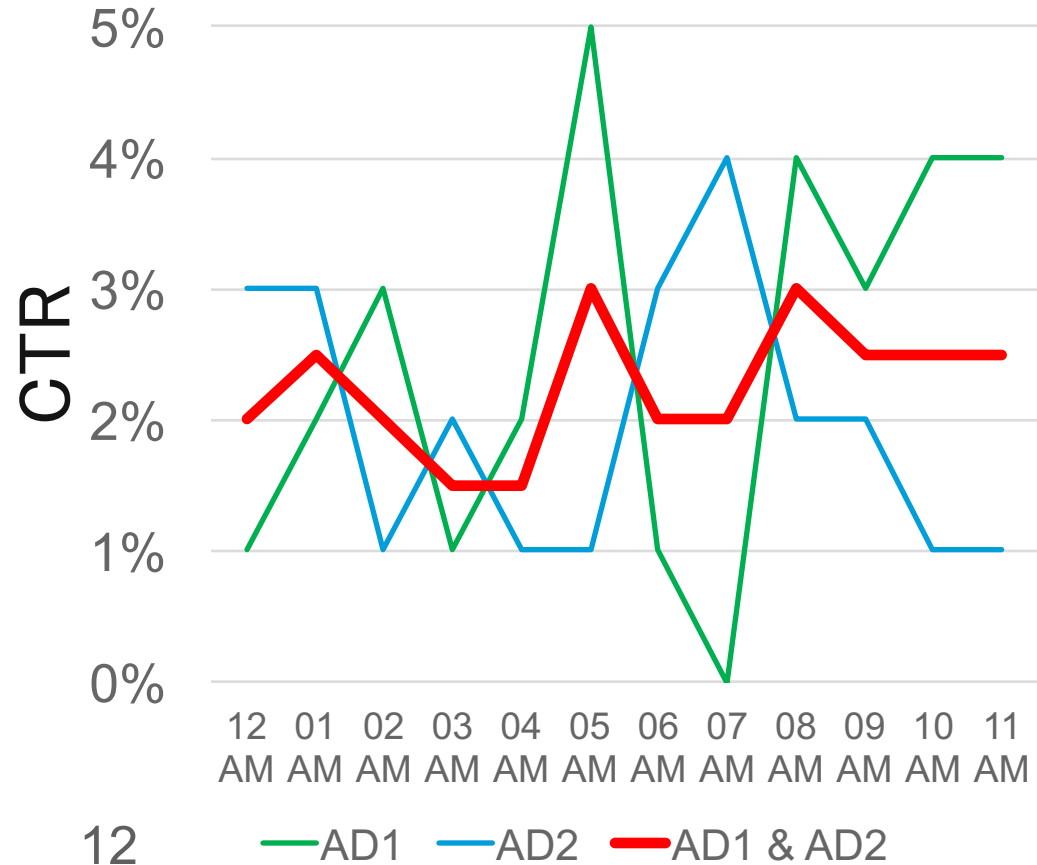
- Display advertising is represented by the **edge-weighted bipartite matching problem**
- Edge weight = CTR (in our research)

CTR: Click Through Rate



# Our Approach: Model and Formulation

- Control the variation rate of CTR
- Find a matching with
  - High CTR
  - Low variation of CTR



# Our Approach: Model and Formulation

- Objective Function as QUBO

$$\arg \max_{\mathbf{x}} \left\{ \mathbb{E} [\mathbf{w}^T] \mathbf{x} - \alpha \mathbf{x}^T W \mathbf{x} - \beta (P \mathbf{x} - \mathbf{1})^2 \right\}$$

**Maximize CTR**      **Low variation**      **Constraint**

$N_a, N_c$  : Size of each vertice

$\mathbf{x} \in \{0, 1\}^{N_a \times N_c}$  : Decision variable

$\mathbf{w} : \Omega \rightarrow \mathbb{R}^{N_a \times N_c}$  : Weights vector (CTR, CVR etc) for each edge

$W \in \mathbb{R}^{(N_a \times N_c)^2}$  : Covariance matrix of  $\mathbf{w}$

$P$  : Matrix which expresses a restriction

$\mathbf{1}$  : Vector with all elements as one

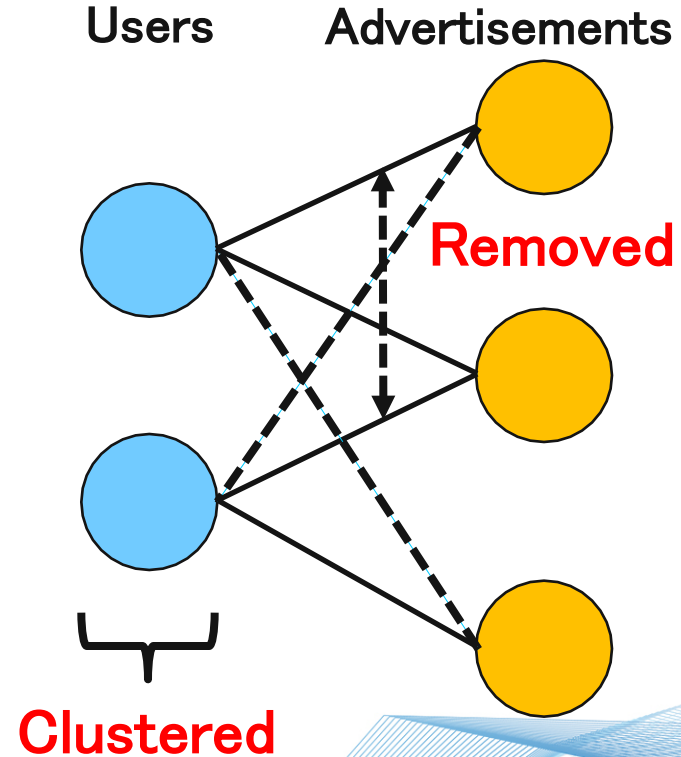
$\alpha, \beta \in \mathbb{R}$  : Control parameters

# Experiments with Real World Data

- Setup
  - Data: our Display Ad campaign data
  - Combination: 14-advertisement campaign and 24 user (cluster)
  - CTR and its variation are estimated by historical data
    - Sample average and variance-covariance matrix

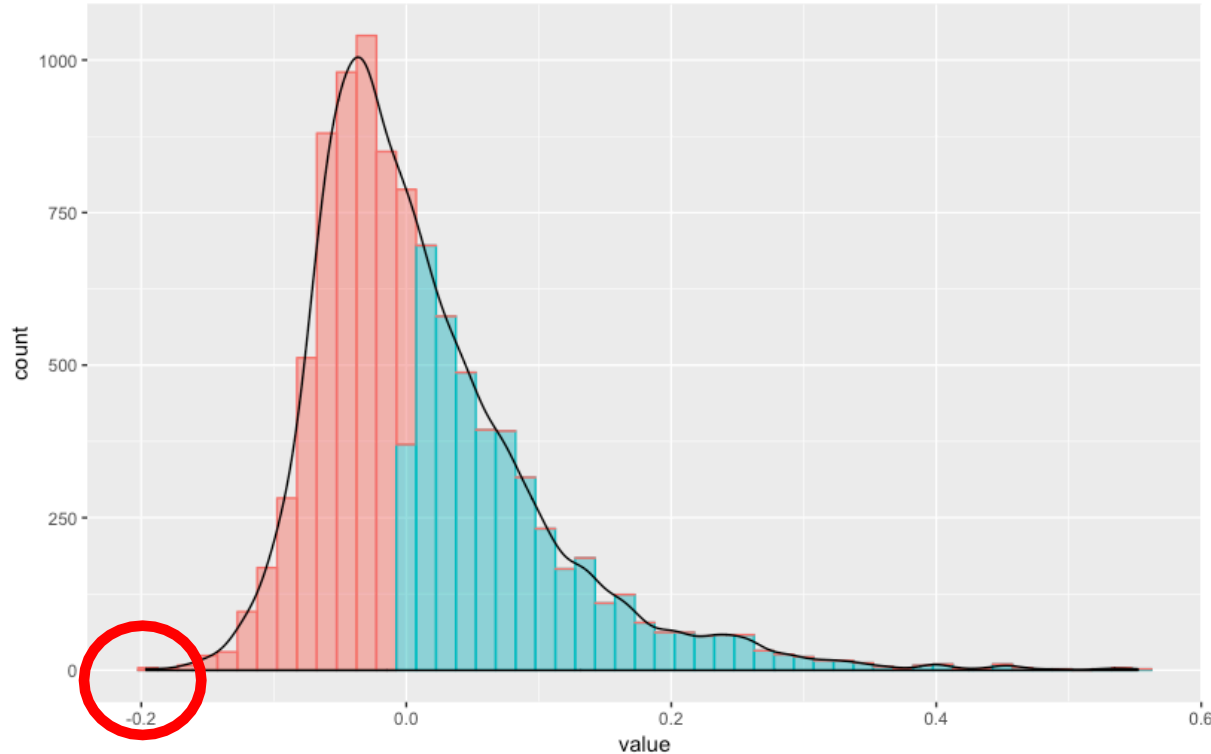
# Experiments with Real World Data

- Use quantum annealing processor, D-Wave 2X
- Some techniques for optimization
  - Pruned edges with less impact
  - Reduce the solution space by clustering users



# Experiments with Real World Data

- Correlation between edges (CTR correlation)





# Performance Measure

Actual CTR

## CTR Matrix

Edge

AD1 x User<sup>1</sup>

AD2 x User<sup>1</sup>

AD3 x User<sup>1</sup>

AD1 x User<sup>2</sup>

AD2 x User<sup>2</sup>

1 : Estimate parameters  
2 : Optimize by D-Wave

Time(Hour)

# Performance Measure

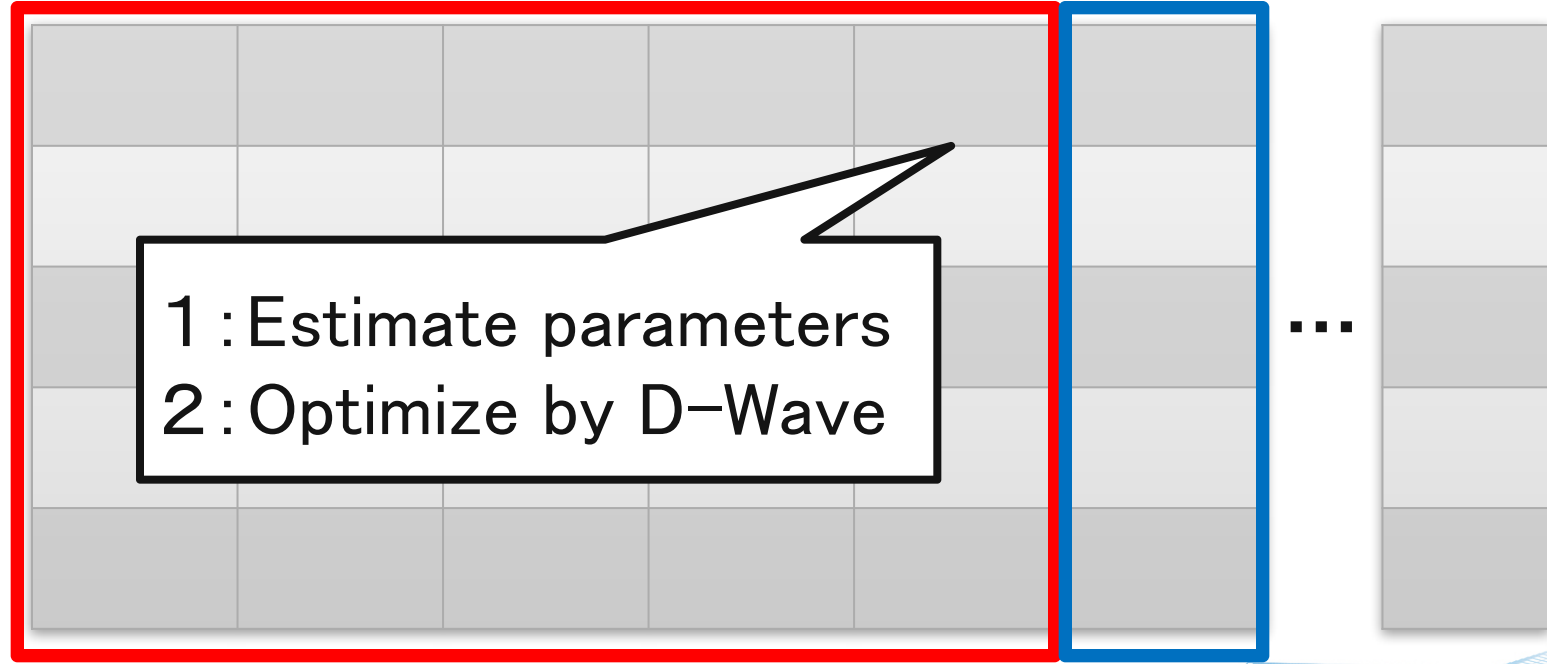
Actual CTR

Edge

## CTR Matrix



AD1 x User<sup>1</sup>  
AD2 x User<sup>1</sup>  
AD3 x User<sup>1</sup>  
AD1 x User<sup>2</sup>  
AD2 x User<sup>2</sup>

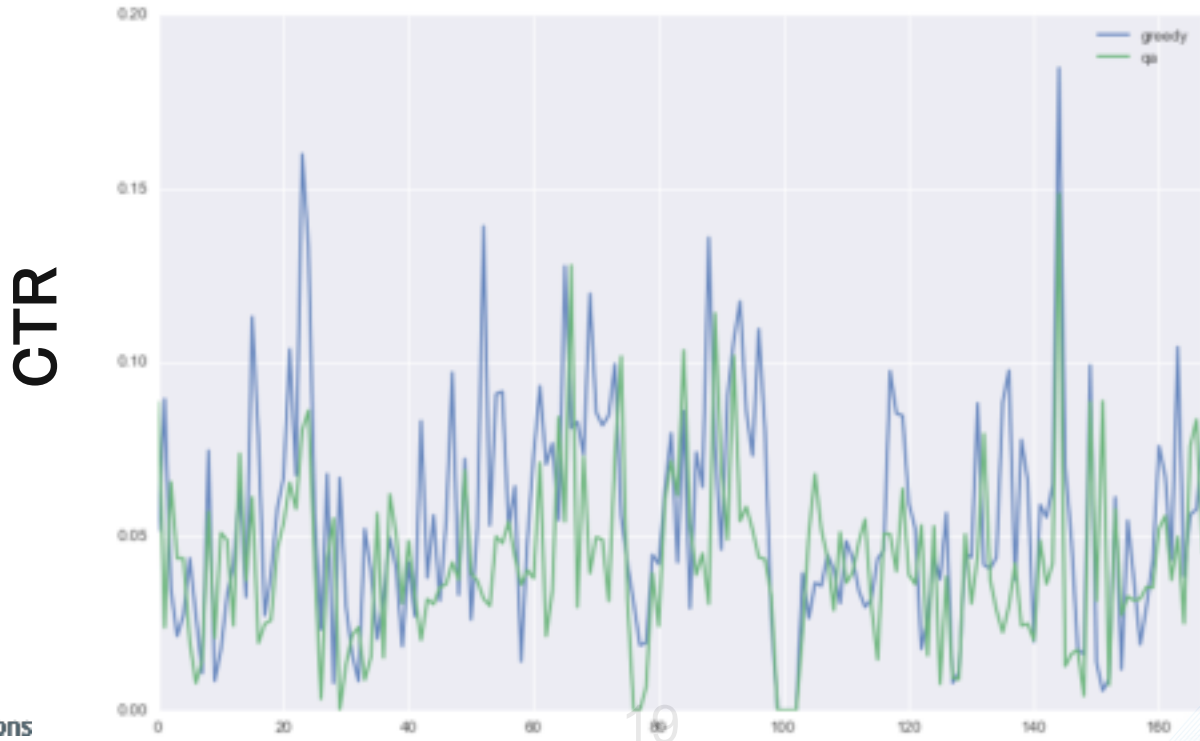


1 : Estimate parameters  
2 : Optimize by D-Wave

Time(Hour)

# Experiments with Real World Data

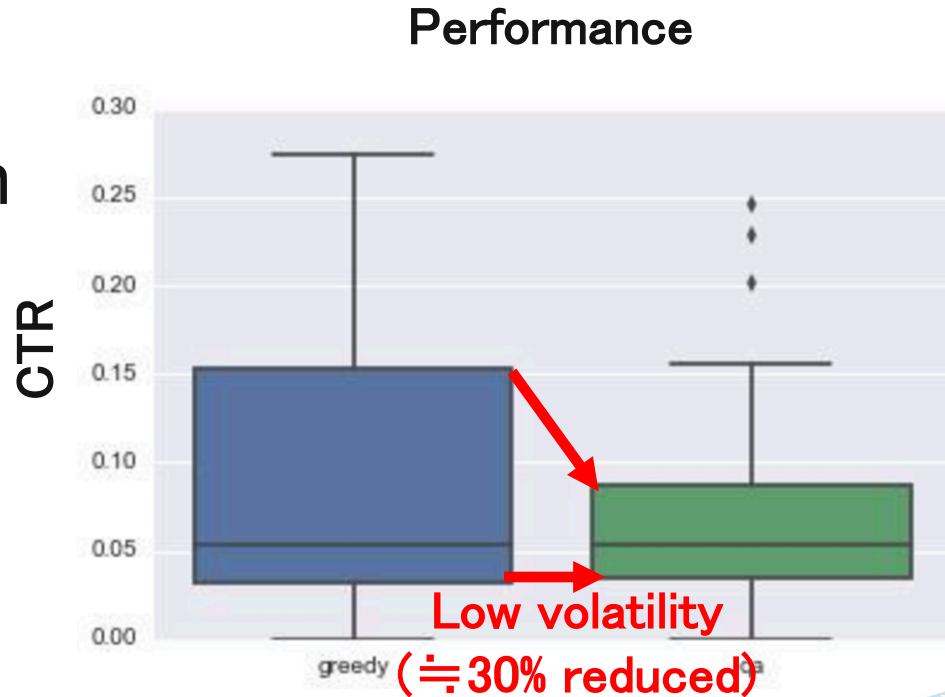
- Hourly performance of each strategy
- Greedy method: Choose maximum CTR edge for each user



— QA  
— Greedy

# Experiments with Real World Data

- Quantum annealing(QA) finds a better solution than the greedy method
  - Almost same CTR level
  - Low variation of CTR



## 4. Summary

- Budget pacing is important for display advertising
- Formulate the problem as QUBO
- Use D-Wave 2X to solve budget pacing control optimization problem
- Quantum annealing finds a better solution than the greedy method.



Thank you for listening



# Memo

# References

1. Budget pacing for targeted online advertisements at LinkedIn
  - D. Agarwal, S. Ghosh, K. Wei, and S. You
  - Proceedings of the 20th ACM SIGKDD, 2014
2. Real time bid optimization with smooth budget delivery in online advertising
  - K.-C. Lee, A. Jalali, and A. Dasdan
  - The Seventh International Workshop on Data Mining for Online Advertising, 2013.
3. Online allocation of display ads with smooth delivery
  - A. Bhargat, J. Feldman, and V. Mirrokni
  - Proceedings of the 18th ACM SIGKDD, 2012.



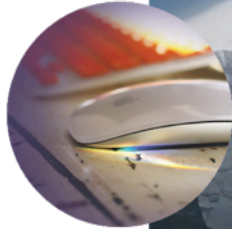
# References

- [Agarwal+ 2014] LASER: A scalable response prediction platform for online advertising, WSDM 2014
- [Ananthanarayanan+ 2013] Photon: Fault-tolerant and scalable joining of continuous data streams, SIGMOD 2013
- [Chapelle+ 2014] Simple and scalable response prediction for display advertising, TIST 2014
- [Graepel+ 2010] Web-scale bayesian click-through rate prediction for sponsored search advertising, ICML 2010
- [He+ 2014] Practical lessons from predicting clicks on ads at Facebook, ADKDD 2014
- [McMahan+ 2013] Ad click prediction : a view from the trenches, KDD 2013
- [Yan+ 2014] Coupled group lasso for web-scale CTR prediction in display advertising,

# HETEROGENEOUS QUANTUM COMPUTING FOR SATELLITE OPTIMIZATION

**GIDEON BASS**  
**BOOZ ALLEN HAMILTON**

September 2017



# Agenda

- **Quantum Annealing in the field**
- **Problem Statement**
- **Results**
- **Conclusions**

# Quantum Annealing has many real-world applications



# However most research has been theoretical

## Traffic flow optimization using a quantum annealer

Florian Neukart<sup>\*1</sup>, David Von Dollen<sup>1</sup>, Gabriele Compostella<sup>2</sup>, Christian Seidel<sup>2</sup>,  
Sheir Yarkoni<sup>3</sup>, and Bob Parney<sup>3</sup>

<sup>1</sup>Volkswagen Group of America, San Francisco, USA

<sup>2</sup>Volkswagen Data:Lab, Munich, Germany

<sup>3</sup>D-Wave Systems, Inc., Burnaby, Canada

### Abstract

Quantum annealing algorithms belong to the class of meta-heuristic tools, applicable for solving binary optimization problems. Hardware implementations of quantum annealing, such as the quantum processing units (QPUs) produced by D-Wave Systems, have been subject to multiple analyses in research, with the aim of characterizing the technology's usefulness for optimization and sampling tasks. In this paper, we present a real-world application that uses quantum technologies. Specifically, we show how to map certain parts of a real-world traffic flow optimization problem to be suitable for quantum annealing. We show that time-critical optimization tasks, such as continuous redistribution of position data for cars in dense road networks, are suitable candidates for quantum computing. Due to the limited size and connectivity

### On the readiness of quantum optimization machines for industrial applications

Alejandro Perdomo-Ortiz,<sup>1,2,3,\*</sup> Alexander Feldman,<sup>4</sup> Asier Ozaeta,<sup>5</sup> Sergei V. Isakov,<sup>6</sup> Zheng Zhu,<sup>7</sup> Bryan O'Gorman,<sup>1,8,9</sup> Helmut G. Katzgraber,<sup>7,10,11</sup> Alexander Diedrich,<sup>12</sup> Hartmut Neven,<sup>13</sup> Johan de Kleer,<sup>4</sup> Brad Lackey,<sup>14,15,16</sup> and Rupak Biswas<sup>17</sup>

<sup>1</sup>Quantum Artificial Intelligence Lab., NASA Ames Research Center, Moffett Field, California 94035, USA

<sup>2</sup>USRA Research Institute for Advanced Computer Science (RIACS), Mountain View California 94043, USA

<sup>3</sup>Department of Computer Science, University College London, WC1E 6BT London, UK

<sup>4</sup>Palo Alto Research Center, 3333 Coyote Hill Road, Palo Alto, California 94304, USA

<sup>5</sup>QC Ware Corp., 125 University Ave., Suite 260, Palo Alto, California 94301, USA

<sup>6</sup>Google Inc., 8002 Zurich, Switzerland

<sup>7</sup>Department of Physics and Astronomy, Texas A&M University, College Station, Texas 77843-4242, USA

<sup>8</sup>Berkeley Center for Quantum Information and Computation, Berkeley, California 94720 USA

<sup>9</sup>Department of Chemistry, University of California, Berkeley, California 94720 USA

<sup>10</sup>IQB Information Technologies (IQBIT), Vancouver, British Columbia, Canada V6B 4W4

<sup>11</sup>Santa Fe Institute, 1399 Hyde Park Road, Santa Fe, New Mexico 87501, USA

<sup>12</sup>Fraunhofer IOSB-INA, Lemgo, Germany

<sup>13</sup>Google Inc., Venice, California 90291, USA

<sup>14</sup>Joint Center for Quantum Information and Computer Science,

University of Maryland, College Park, Maryland 20742, USA

<sup>15</sup>Departments of Computer Science and Mathematics,

University of Maryland, College Park, Maryland 20742, USA

al Security Agency, Ft. George G. Meade, Maryland 20755, USA

USA Ames Research Center, Moffett Field, California 94035, USA

(Dated: September 1, 2017)

monstrate that quantum annealing and, in particular, quantum annealing the potential to outperform current classical optimization algorithms he benchmarking of these devices has been controversial. Initially, however, these were quickly shown to be not well suited to detect benchmarking shifted to carefully crafted synthetic problems designed

The background features a stylized globe with a grid of latitude and longitude lines. Overlaid on this are numerous white, glowing lines representing satellite orbits, which crisscross the globe in various directions, creating a complex network of paths. The globe is centered in the frame, and the orbits are most prominent in the upper and lower quadrants.

# Satellite Coverage Quantum Optimization

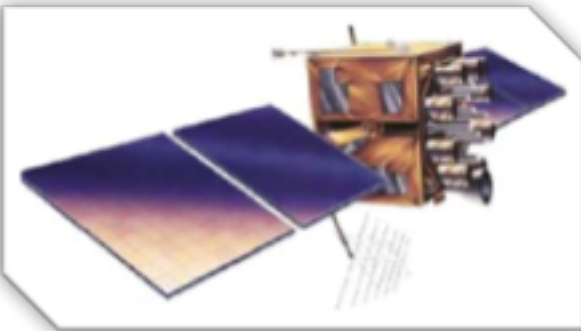
# Satellite Coverage Optimization

**Summary:** Group satellite together in such a way as to maximize coverage.

**Data:** For any possible grouping of satellites, a coverage percentage

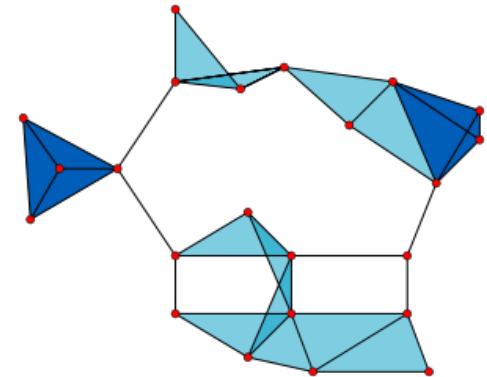
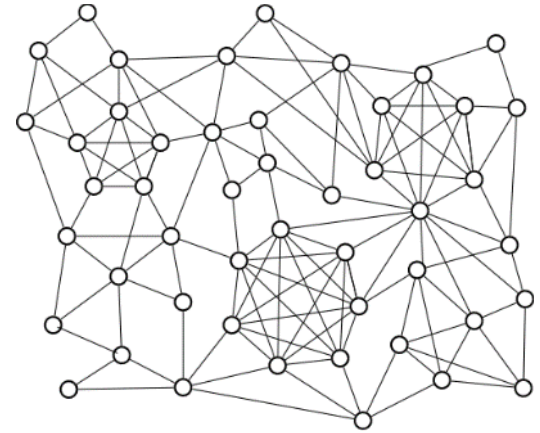
**Goal:** Assign each of  $N$  satellites to  $k$  groups, such that total mean coverage is maximized

- Satellites change position and **require constant re-optimization**
- **Brute force solving is out of the question;** even trivial subsets of the satellites form too many combinations to check.
- Quantum technology offers a promise to **perform combinatorial optimization much faster**, while yielding better coverage outcomes.



# The weighted k-clique problem

- This problem can be reformulated as a graph problem, called the **k-clique problem**
- Each potential group of satellites in a sub-constellation can be considered a node on a graph
  - Each node is given a weight equal to the coverage provided
  - If both sub-constellation use the same satellite, the nodes are unconnected
  - The goal is thus to find the k nodes with the highest total weight that are all mutually connected (a "clique")
- This problem can then be expressed as a QUBO, and sent to the quantum computer





# Designing the QUBO

Constraints:

1. Choose only nodes that are connected
2. Maximize the sum of coverages for each group chosen
3. Choose a number of qubits equal to the number of available satellites

Each (logical) qubit represents a potential grouping of satellites

Connections represent a grouping that is non-overlapping (does not use the same satellite in multiple groups)

$$H = \sum_{i < j} 2(w_i + w_j)$$

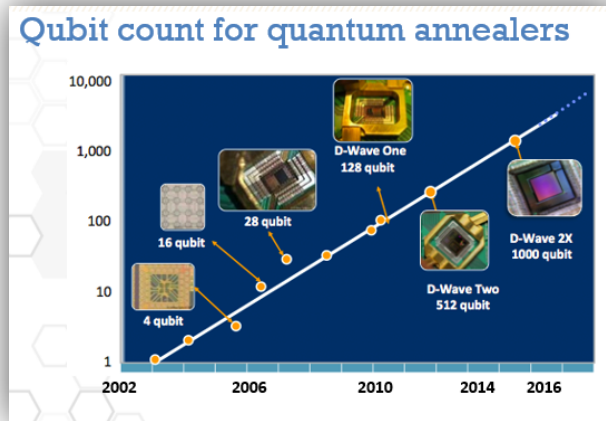
$$H = \sum_i -Aw_i x_i$$

$$H = W \left( \sum_i x_i - 8 \right)^2 = 64W - \sum_i 8W x_i + \sum_{i < j} x_i x_j$$

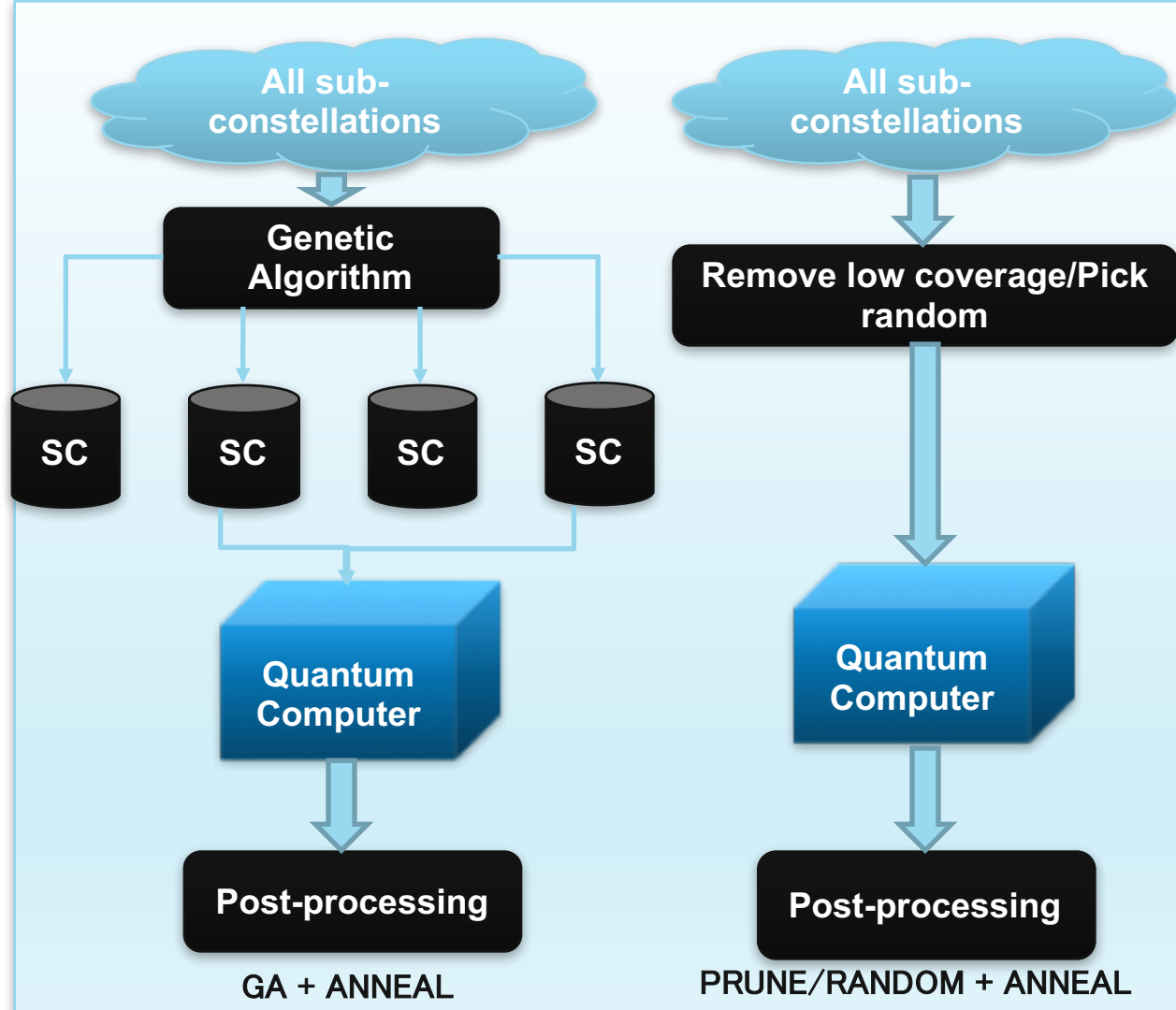
**W is the qubit maximum weight**

# Quantum Hardware is rapidly maturing

- This satellite optimization problem is a **prime candidate for a quantum approach** when used in concert with classical computing resources.
- The application to satellites could be **the first major quantum success** when applied to a real-world full-scale problem.
- However, with current numbers, we would still need  $10^4$ - $10^5$  qubits to fully embed this problem
- Thus, we created a heterogeneous approach that combines classical processing and quantum annealing



# Heterogeneous techniques: TWO APPROACHES



# Heterogeneous Computing Models

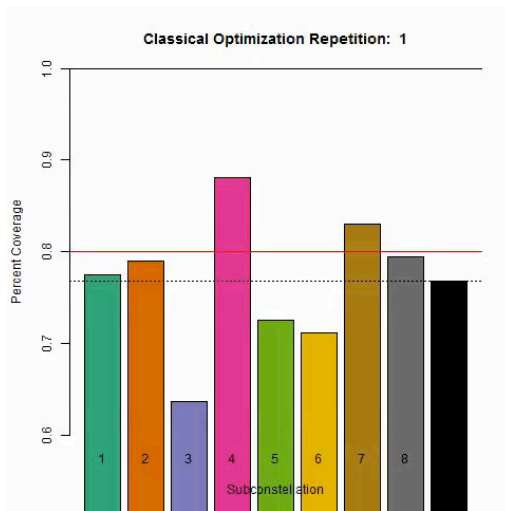
Method	Pros	Cons
Classical Heuristics	Can provide fairly good results. Can be run on classical machine.	Cannot be run on current QA devices, no quantum speed-up, scaling uncertain
GA pre-processing	Searches full decision space, produces solid results	Middle of the road performance and speed, many parameters to tune
Prune and Anneal	Very good results in good time, most similar to existing technique	Does not explore full solution space, requires domain knowledge

# Results

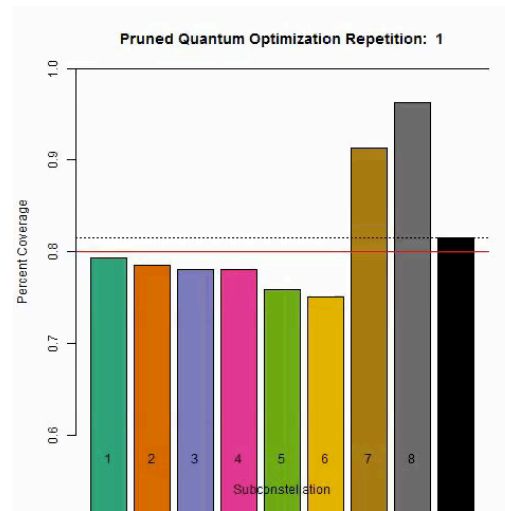
## Comparison:

### Quantum Simulator

- An 80% coverage(**red**) is the minimum acceptable average.
- The eight colored bars represent individual sets, black bar (and dotted line) is overall average
- Quantum approach is faster and finds a significantly better results

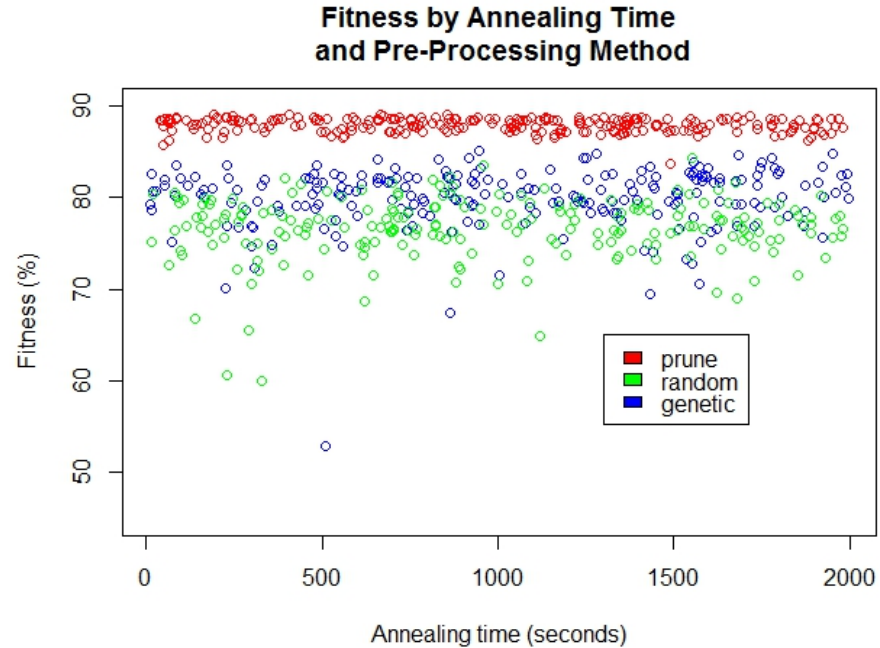


Purely Classical Genetic Algorithm



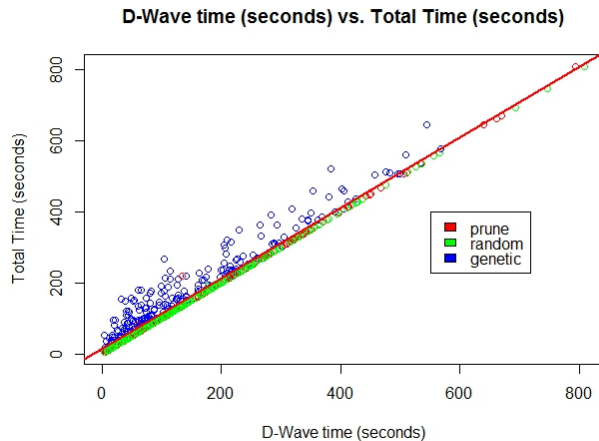
Simulated Quantum Prune and Anneal

# Results Comparison: D-Wave



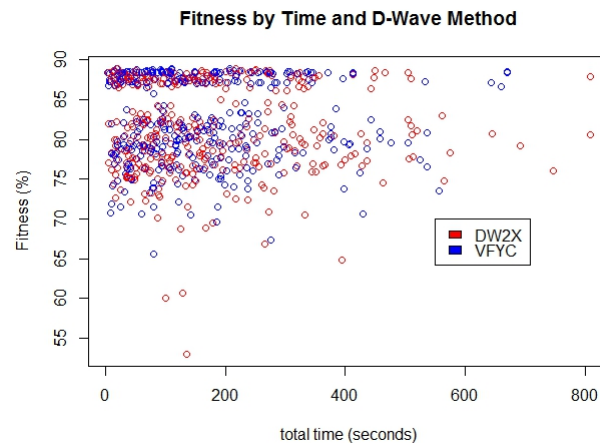
- Results are nearly constant with processing time
- Results are highly dependent on pre-processing method (color)
  - 80% is minimal acceptable
  - 90% is likely near the true maximum.

# Results Comparison: D-Wave



- D-Wave time makes up most of the time, GA adds a little more

- Including D-Wave's "Virtual Full Yield" does not significantly change performance while improving portability



# Summary

Method	Uses Domain-Knowledge	Time Needed	Performance
Prune + Anneal	✓	Very Little	90%
GA + Anneal	X	Some	80-85%
Random + Anneal	X	Very Little	75-80%

- The D-Wave functions best as a co-processor
- Performance is highly dependent on problem formulation, classical processing step
- Quantum portion does appear to provide significant improvement.



# Conclusions

- As problems and datasets grow, modern computing systems have had to scale with them. **Quantum computing offers a totally new and potentially disruptive computing paradigm.**
- For problems like this satellite optimization problem, **heterogeneous quantum techniques will be required to solve the problem at larger scales.**
- Preliminary results on this problem using heterogeneous classical/quantum solutions **are very promising.**
- Exploratory studies in this area **have the potential to break new ground** as one of the first applications of quantum computing to a real-world problem

# Thank You

GIDEON BASS

BOOZ ALLEN HAMILTON

